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We look at a sufficiently small time interval  $[t, t + \Delta t]$

$\Delta x, \Delta y$  = the change of amount of salt in Tank A and Tank B, respectively, in  $[t, t + \Delta t]$

$20 \Delta t$  = the amount of solution flowing into Tank A & B, respectively, in  $[t, t + \Delta t]$

$\frac{x(t)}{200}, \frac{y(t)}{300}$  = density of salt in Tank A & B, respectively, at time  $t$  (or approximately in  $[t, t + \Delta t]$ )

$$\Delta x = \underbrace{-20 \Delta t \frac{x}{200}}_{\text{flow out}} + \underbrace{20 \Delta t \frac{y}{300}}_{\text{flow in}}$$

↓ divided by  $\Delta t$

$$\frac{\Delta x}{\Delta t} = -\frac{1}{10}x + \frac{1}{15}y \quad \text{let } \Delta t \rightarrow 0$$

$$x' = -\frac{1}{10}x + \frac{1}{15}y$$

Similarly, we can derive

$$y' = \frac{1}{10}x - \frac{1}{15}y$$